

LIGO (5 points).

The first detection of gravitational waves GW150414 was announced in 2016 by the collaboration LIGO (Laser Interferometer Gravitational-Wave Observatory). The detected signal corresponds to the merger of two black holes with masses of $35M_{\odot}$ and $30M_{\odot}$, which when joined formed a black hole of $62M_{\odot}$. Ignoring the rotational energies of the black holes, you may assume that the energy released by this process (E_{GW}) is emitted solely in the form of gravitational waves, that were observed by the interferometer in 2015. You are given that the explosion of a supernova (SN) releases $E_{SN} = 2 \times 10^{44} J$.

1.1	To find out which of these two events (SN, GW) releases more energy, estimate the energy ratio $\frac{E_{SN}}{E_{GW}}$.	5.0pt





Temperature of the Earth (10 points).

For at least the last few million years, the Earth has been in roughly thermal equilibrium with the radiation from the Sun at the Earth's orbital distance.

- **2.1** Assuming our planet to be an ideal black body, calculate what the Earth's equilibrium temperature (in Celsius) would be.
- **2.2** The Earth's albedo is approximately 30%. Calculate the Earth's surface temper- 2.0pt ature (in Celsius) considering its albedo.
- 2.3 The Earth's absorbed radiation is reemitted as black body radiation from its surface, but its atmosphere re-absorbs 58% of that energy, causing a greenhouse effect. Considering this effect, calculate the Earth's surface temperature (which will be the same as the temperature of the lower atmosphere). Give your answer in Celsius.
 For simplicity, consider the reabsorption effect as bappening only once, and do

For simplicity, consider the reabsorption effect as happening only once, and do not consider the atmosphere as a separate black body.





Mars (10 points).

A spacecraft of mass $m=5.0 \times 10^4 kg$ approaches in a parabolic orbit AB, with respect to Mars. When the spacecraft reaches point B of least distance to the center of Mars, $r_B = 6.8 \times 10^6 m$, it undergoes an instantaneous deceleration using its rockets and goes into a perfectly calculated orbit so that it will touch the Martian surface exactly at point C, diametrically opposite B, as shown in the figure.



- 3.1 Determine the speed (km s⁻¹) of the spacecraft at point *B* just before the decel- 3.0pt eration.
 3.2 Calculate the total energy (*J*) of the spacecraft as it is moving between points B 4.0pt and C.
 - **3.3** Calculate the speed ($km s^{-1}$) of the spacecraft at point *C*. 3.0pt





ALMA - Calculating photons (10 points).

ALMA is a radio observatory with a revolutionary design. It consists of 66 high-precision antennas, operating in the wavelength range from 0.32 mm to 8.60 mm. The principal array has fifty antennas of 12 m diameter each that can work together as a single telescope in the so-called interferometric mode. There is also another array of four 12 m antennas, and twelve smaller antennas of 7 m diameter each.

Imagine that a single $12\,m$ antenna is being calibrated, pointing to a source with a known incident flux of $1\times 10^{-20}\,W/m^2$

4.1	Assuming that all the flux arrives at the shortest wavelength of ALMA sensitivity,	2.0pt
	determine the average number of photons that would reach the detector every	
	second.	

- **4.2** Compare it to the average number of photons that would have reached the 2.0pt detector, if all the flux arrived at the longest wavelength of operation.
- **4.3** What is the angular resolution (in arcsec) of a single 12 *m* antenna, operating at 2.0pt 74.9 *GHz*?
- **4.4** Imagine the principal array operating at 74.9 GHz in the interferometric mode. 2.0pt Assuming for simplicity that the spatial resolution is solely given by the longest baseline (largest distance between any pair of antennas), which turns to be $D_{max} = 16 \ km$, what would be the angular resolution (in arcsec) in this case? Treat this case as a single slit aperture instead of a circular one.

4.5	For a radio antenna, the term SEFD refers to 'System Equivalent Flux Density',	2.0pt
	temperature and size. We also note that for energy estimation of radio pho-	
	tons, Rayleigh-Jeans approximation is valid. Assuming a system temperature	
	of $691 K$, what would be the SEFD of the full ALMA observatory in Jansky if all	
	the 66 antennas could work together?	





Under pressure (10 points).

Magnetic fields in the Sun are constantly shaping the structure of various different features in the Solar atmosphere. Inside any feature, the magnetic field (*B*) adds to the total pressure exerted by the gas. This so-called magnetic pressure is a function of the height *z* and can be expressed as:

$$P_{mag}(z) = \frac{B^2(z)}{2\mu_0}$$

On the other hand, the gas can be considered to be in hydrostatic equilibrium and hence the gas pressure decays exponentially from an initial pressure value P_0 with increasing *z*. It can be expressed as,

$$P_{gas}(z) = P_0 e^{-z/H}$$

where H is the scale height, i.e. the height at which the pressure falls to $\frac{P_0}{e}$.

Consider one type of feature, a magnetic flux tube rising from the Solar surface up into an unmagnetized environment (see Figure below). Assuming that the total pressure of the material inside the tube and of the material outside it is in equilibrium,



- **5.1** Find an expression for the magnetic field strength as a function of height *z*. 7.0pt
- **5.2** If the magnetic field at the base of a flux tube is 0.3T, and scale height *H* in a 3.0pt given solar model is 150 km, at what height will the magnetic field be reduced to 0.03T?



Macondo and Melquiades (12 points).

In 2019, as a part of the NameExoWorlds campaign of the International Astronomical Union, Colombia was granted an opportunity to select a name for the star HD 93083 and its planetary system. HD 93083 is a K - type dwarf star and has one extrasolar planet orbiting it. Today they are officially known as Macondo (star) and Melquiades (planet), from the literary ideas of the Colombian writer Gabriel García Márquez.

This star has an effective temperature of 4995 K and an apparent visual magnitude of 8.3. As per GAIA DR2, the parallax for Macondo is 35.03 milliarcseconds. You may assume the orbit of Melquiades is perfectly circular. In the figure you can see the plot of radial velocity of Macondo with respect to the phase.



Radial velocity of Macondo (Y-axis in $km s^{-1}$) as a function of the phase (X-axis).

6.1	Find the wavelength $(innm)$ of peak emission for Macondo in its rest frame (i.e., ignoring Doppler shifts).	2.0pt
6.2	Find the distance of this system from the Earth (in parsecs) and the absolute visual magnitude (M_V) of the star.	2.0pt
6.3	Calculate the mean radial velocity of Macondo (in $km \ s^{-1}$).	2.0pt





- **6.4** Calculate the orbital velocity (in km/s) of Melquiades (v_p) , if mass of the star 2.0pt (m_s) is 0.7 M_{\odot} and the mass of exoplanet (m_p) is $7 \times 10^{26} kg$. Assume that the orbital plane of the system is edge-on with respect to our line-of-sight.
- **6.5** Find the orbital radius of Melquiades (in *au*) and its orbital period (in days). 4.0pt





Menkalinan (β Aurigae) (13 points).

Almost half of the stars that we see are either binary or multiple star systems. A well-known example of this is Menkalinan (Beta Aurigae), which was initially thought to be a single star, but today recognised as a binary system comprising two stars that we will refer to as Menkalinan A and B. In the following figure, a spectrum of the system (obtained by the observatory of the Universidad de los Andes, in Bogotá) is shown:



Spectrum of Menkalinan binary system in the region of $H\alpha$. Y-axis is for the relative flux, and X-axis measures wavelengths. Menkalinan A is marked as A in the graph, and Menkalinan B is marked as B.

Answer the following questions using the plot and noting that the wavelength of $H\alpha$ line in the laboratory frame is 656.28 nm. Assume circular orbits, and assume that the binary system as a whole is at rest with respect to the observer.

- **7.1** In the spectrum, we can see the $H\alpha$ line for each star in the system. Calculate 5.0pt the line-of-sight velocity of each star (km/s) and determine, at the time of this observation, which of the two stars is moving towards us.
- **7.2** The binary system is located 81.1 light years from Earth and has an orbital period 4.0pt of 3.96 days. The semi-major axis for Menkalinan B (smaller star) was measured to be 3.35 *milliarcseconds*. If the mass ratio of the two components is 1.026, find the total mass of the system (in solar masses).





7.3 Calculate the individual masses of Menkalinan A and B in solar masses.2.0pt**7.4** Since Menkalinan A and B are main sequence stars, use the relation:2.0pt $\frac{L}{L_{\odot}} = (\frac{M}{M_{\odot}})^{3.5}$

to estimate the luminosity of each star (in solar luminosity).



IOAA Logo (15 points).

The IOAA2021 logo is formed by the acronym IOAA, where the first letter is represented by the silhouette of the building of the National Astronomical Observatory (OAN) of Colombia, the oldest observatory in America. This observatory is located in Bogota, where it was founded in 1803. The capital city of Colombia is bordered by two famous hills, Monserrate and its neighbor Guadalupe, which are icons of Bogota's cityscape that decorate the logo's background.





Aerial view of Bogota City. Numbers show locations for the quoted places: 1 is for OAN; 2 is for Guadalupe; and 3 is for Monserrate.





Point	Latitude	Longitude	Elevation (m.a.s.l)
1	$4^{\circ} 35' 53'' N$	$74^\circ04'37''W$	2607
2	$4^{\circ} 35' 30'' N$	$74^{\circ} \ 03' \ 15'' \ W$	3296
3	$4^{\circ} \ 36' \ 18'' \ N$	$74^{\circ} \ 03' \ 19'' \ W$	3100

8.1 Estimate the distance (in km), between points 2 (Guadalupe) and 3 (Monserrate). 3.0pt

- **8.2** Estimate the angular separation (in degrees) between Guadalupe (2) and Monserrate (3) as observed from the National Astronomical Observatory of Colombia (1).
- **8.3** From the OAN, on September 21 at 8:00 p.m. the Moon was observed towards 6.0pt the eastern hills (between Monserrate and Guadalupe). The measured ecliptic coordinates (longitude and latitude) of the Moon are shown in the table. Determine the equatorial coordinates of the Moon at the time of observation.









Local Time: 8:00 p.m.

 $\begin{array}{l} Az:+90^{\circ}42'59''/Alt:+19^{\circ}01'42''\\ \lambda:+12^{\circ}20'16''/\beta:-04^{\circ}24'14'' \end{array}$

Note: Azimuth measured from North to East.

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Pluto Satellites (15 points).

9.1 The mass of Charon, the biggest satellite of Pluto, is 1/8th the mass of Pluto. 15.0pt Both bodies move in a circular orbit around a common center of mass. In addition, they both are tidally-locked.

The distance between the center of the planet and the center of the satellite is $R = 19\ 640\ km$ and radius of the satellite is $r = 593\ km$.

Let g_0 be the gravitational acceleration on the surface of Charon due only to its mass.Let A be the point on Charon surface directly facing Pluto, and B the point diametrically opposite. Compute the percentage difference between gravitational acceleration at A and B respect to g_0 .





Terrestrial Transit (15 points).

Note: Assume perfect circular orbits in both questions below.

- **10.1** An alien astronomer from a distant planetary system is observing the Sun. Suddenly, the brightness of the Sun drops due to the transit of the Earth in front of it. What is the maximum duration that this transit may last (in hours)? Assume that the planet where the astronomer observes from, does not move relative to the Sun.
- **10.2** Imagine that the transit of a given exoplanet as seen from Earth lasts 31 minutes. The host star is a red dwarf, with mass and radius that are 10% of the mass and radius of the Sun. What is the minimum orbital period this exoplanet may have (in days)?





Minimum velocity of a projectile (15 points).

- **11.1** What is the minimum speed with which a projectile must be launched from the 12.0pt Earth's surface at the equator such that the projectile reaches the north pole?
- **11.2** Find the eccentricity of the trajectory described by the projectile 3.0pt

You may ignore the rotation of the Earth. Also assume the earth surface is spherical.







Hodograph (15 points).

In curvilinear motion of a planet around a star, the direction of the velocity vector changes continuously. This can be represented by a so-called "trajectory in velocity space" and is obtained as follows: for each point on the spatial trajectory, the corresponding velocity vector is drawn so that its starting point is at the origin of the velocity space, and its magnitude and direction is the same as the velocity vector at that point. The tip of this variable velocity vector generates a curve in velocity space. (The name 'hodograph' was given to this curve by Hamilton in 1846.)

As an example, see figures 1 and 2 below. For a circular orbit (Figure 1), the magnitude of the velocity is constant and therefore, the hodograph (Figure 2) of the velocity vector for Keplerian circular motion is also a circle, the center of which is located at the origin of the velocity space. The radius of this circle is equal to the constant magnitude of the circular velocity.



Fig. 1 Spatial trajectory of the Planet with Uniform Circular Motion around the star.







- **12.1** Write an expression for the radius of the hodograph in Fig. 2, as a function of 1.0pt the mass M of the star, and the radius R of the circular orbit of the planet's motion.
- **12.2** For a planet in a Keplerian trajectory, write the expression for centripetal acceleration vector (\vec{a}) and the magnitude of angular momentum (L). For any Keplerian trajectory, it is true that

$$|\Delta v| = k\Delta \theta$$

(1)

Where k is a constant for each type of Keplerian trajectory. Find the expression for the constant k as a function of the masses M and m of the star and the planet, respectively, and the angular momentum, L. (Eq.1) allows us to conclude that for any Keplerian trajectory, the hodograph

 $(v \text{ as a function of } \theta)$ is a circle, but except for circular motion, the centre of the hodograph does not coincide with the star. It is not necessary to prove this result, you may simply accept it as a given. For the hodograph of uniform circular motion, the compliance with (eq.1) is completely obvious, as evidenced in Fig. 3

7 velocity space

Fig. 3

12.3 Determine the expression of the constant k for the hodograph of circular plan- 2.0pt etary motion.





- - 12.5 Similarly, for the parabolic Keplerian trajectory, determine the radius of the corresponding hodograph and the distance from the center of that hodograph circle to the star. Express the radius as a function of the velocity at periastron. Draw a rough sketch of the hodograph circle in the answer sheet.



English (Official)

Lucy: The First Mission to the Trojan Asteroids (15 points).

CCD cameras on space probes are very sensitive and exposed to space weather conditions. Intense radiation passing through the CCD produces electron-hole pairs in the silicon of the CCD chip. The rate at which these pairs are produced is an important parameter when operating cameras on board spacecraft and can be calculated for radiation of any given energy.

A high energy particle or photon of radiation passing through the CCD will deposit some energy in the chip with each electron-hole pair it creates. The 'stopping power' of silicon for a given type of particle can be measured as the energy per areal density (*areal density* = mass per unit area) that the silicon 'takes away' from the travelling particle.

NASA's Lucy mission will be the first to study the Trojan asteroids and will revolutionize our understanding of the formation of the Solar System. One of the instruments on board is L'LORRI (Lucy LOng Range Reconnaissance Imager), which contains a sensitive CCD in order to produce detailed images of the Trojan asteroids. Unfortunately, the radiation around Jupiter is very intense and it can generate a lot of 'noise' in the pixels of the CCD.

Let us assume that an average charged particle trapped in Jupiter's magnetic field has an energy of $15 \ MeV$ and that the flux of such particles in this region is equivalent to about 600 electrons $s^{-1} \ cm^{-2}$. Also assume that for each electron-hole pair which a particle passing through a pixel creates, it deposits exactly the excitation energy of the pair in that pixel. After the pixel crosses a threshold number of electron-hole pairs it is 'excited' and no more pairs can be produced in that pixel. Any remaining energy in the particle is passed to the next pixel (and so on).

Using the data given below for the CCD chip in the L'LORRI camera, answer the following questions:

- **13.1** How many pixels will be excited by one such particle of radiation passing 10.0pt through the CCD when the spacecraft is near Jupiter's orbit?
- **13.2** Given the radiation flux near Jupiter, what percentage of the total number of 5.0pt pixels in an image will be excited?



Q13-2 English (Official)

CCD Data:

- Exposure time of an image = 30 ms
- Pixels on the CCD = 1024 x 1024
- CCD Area = 13 mm x 13 mm
- CCD chip thickness = 0.06 cm
- Density of silicon, ρ = 2.34 g cm⁻³
- Excitation energy of single pair = 2.36 eV
- Excitation threshold of a single pixel = 250 pairs
- Stopping power' of silicon for a 15 MeV electron = 3.012 MeV g⁻¹ cm²





English (Official)

Formation of the Venus-2 (35 points).

A comet of mass αm is heading ("falls") radially towards the Sun. It is known that the total mechanical energy of the comet is zero. The comet crashes into Venus, whose mass is m. We further assume that the orbit of Venus, before the collision, is circular with radius R_0 . After the crash, the comet and Venus form a single object, called "Venus-2".



- **14.1** Find the expression in terms of M_{sun} and R_0 for the orbital speed, v_0 , of Venus 1.0pt before the collision.
- **14.2** Find an expression for the total mechanical energy of Venus in its orbit before 1.0pt colliding with the comet.

14.3 Find an expression for the radial velocity, v_r , the angular momentum, L, of 10.0pt "Venus-2" immediately after the collision.

- **14.4** Find an expression for the mechanical energy of the combined object "Venus-2" 5.0pt and express it in terms of energy before the collision, E_i , and α .
- **14.5** Show that the post-collision orbit of "Venus-2" is elliptical and determine the 5.0pt semi-major axis of the orbit.

14.6 Determine if the year for the inhabitants of "Venus-2" has been shortened or lengthened because of collision with the comet. Write the ratio between the period of Venus-2 and Venus.





- **14.7** What should be the value of α such that the post-collision orbit of Venus-2 would 5.0pt make it crash in the Sun? We will call this as α_c
- **14.8** A comet with $\alpha = \alpha_c$ collided with Venus. Calculate the percentage change in 5.0pt the magnitude of Venus' velocity (δv) and the change in the direction of the velocity vector ($\delta \theta$) immediately after the collision.





Data Analysis 1: Scaling Relations (75 points)

Please read the general instructions in the separate envelope before you start this problem.

Spiral galaxies are disk-like rotating structures, whose dynamical state is fairly grasped by the so-called rotation curves, quantifying the mean rotational velocity of the disk at different distances from the center (see Figure 1, curve B). An interesting feature is the flat region of the curve, which is attributed to the presence of dark matter. Without it, rotation velocities would drop steadily at large radii from the center, as depicted in curve A.



Figure 1: Rotation curves. Circular velocity (Y-axis) vs Radius (X-axis)

In disk galaxies a strong correlation has been observed between the intrinsic luminosity of the whole galaxy and the asymptotic rotational velocity (as given by the rotation curve for the outer edge of the galaxy i.e. $R_{\rm max}$), a result that is known as the Tully-Fisher relation. This relation also holds if you use the luminosity in a specific band. This is shown on Figure 2 for a number of galaxies in a galaxy cluster. Every dot is a galaxy, and the solid line is the best-fit linear relation between absolute magnitude in K band and $log_{10}(V_{\rm max})$ for the whole sample.



Figure 2: Absolute magnitude in K band vs $\log_{10}(V_{\max}[kms^{-1}])$. Tully-Fisher relation for several galaxies. Every dot represents a galaxy. The dark points are five selected galaxies, for which we will provide some numbers in part 1.2.







Figure 3: Gas fraction vs stellar mass.

Another interesting trend is shown in Figure 3: disks with larger stellar masses (M_*) tend to have smaller gas fractions (M_{aas}/M_*).

In the following questions you will be asked to extract physical information about the galaxies using the scaling relations just introduced. Consider the following guidelines:

- Assume that V_{max} was measured at the same radius for all galaxies (R_{max}), in the flat part of the rotation curves and well beyond the end of the stellar disk.
- Use M_{dm} for the dark matter mass up to R_{max} and M_{tot} for the sum of all components.(gas, stars and dark matter)
- Assume that all galaxies have identical stellar populations¹, and assume that the gaseous component does not interact with the stellar light. .
- The galaxy cluster is far away. Its distance is much larger than the cluster size.
- In spherically-symmetric mass distributions, to infer the gravitational effect on a particle at distance r from the center, it suffices to consider the total mass enclosed up to that radius $M(\leq r)$ as if it were placed at the very center of the distribution.





¹The term stellar population refers to the type of stars that are present in a galaxy, and the relative amount of each type with respect to the total number of stars.

Part 1 (20 points).

1.1 From an analysis of Figure 3, find the appropriate constants in the following 5.0pt relation: $M_{gas} = a \times M_*^b$

a = ?

- b = ?
- **1.2** In the plot of the Tully-Fisher relation there are 5 highlighted points. Data for these 5 galaxies is given in the following table. Use this dataset to find the appropriate constants for TF relation presented below the table, by means of a linear fit using the method of least squares.

Note: Treat $log_{10}(V_{max})$ as the x variable and K as the y variable in the linear fit.

$V_{\sf max}[km/s]$	K[mag]
79.4	-16.8
100.1	-19.2
158.5	-21.3
251.2	-21.4
316.2	-24.0

 $K = c \times log_{10}(V_{max}) + d$

d = ?

c = ?

Part 2 (16 points).

2.1

For two galaxies, G1 and G2, in the cluster, the recorded *apparent* magnitudes are:

$$k_1 = 19.2$$
 ; $k_2 = 25.2$

Using this information and the relations calibrated in Part 1 find the correct exponents in the following equations:

$$\frac{M_{*1}}{M_{*2}} = 10^e \qquad ; \qquad e = ? \end{tabular}$$
 6.0pt





2.2	$\frac{M_{gas1}}{M_{gas2}} = 10^f \qquad ; \qquad f = ?$	4.0pt
2.3	$\frac{M_{tot1}}{M_{tot2}} = 10^g \qquad ; \qquad g = ?$	6.0pt

Part 3 (15 points).

Galaxy	Apparent magnitude <i>k</i>	$M_{gas}[M_{\odot}]$	$M_{*}\left[M_{\odot}\right] M_{dm}[M_{\odot}]$	$M_{tot} \; [M_\odot]$
G_1	19.2			4.39×10^{11}

Part 4 (24 points).

4.1 Consider a systematic uncertainty of $\sigma_{sys} = \pm 0.2$ in each apparent magnitude 4.0pt due to CCD calibration errors. Then k_1 must be read as $k_1 = 19.2 \pm 0.2$, i.e., the only thing we know is that k_1 most likely lies in the interval [19.0, 19.4]. The same goes for k_2 . Recalculate the exponent in the scaling relation $\frac{M_{s1}}{M_{s2}} = 10^e$ (found in 2.1), expressing e as an interval estimated by considering the extreme possible variations in k_1 and k_2 .

 $e~\in~[?,?]$





4.2 Now we consider that there is always a natural spread of the data around any relation. For instance, for a given value of the *K* magnitude the TF relation gives a single value of $log_{10}(V_{\text{max}})$, but it would be more realistic to report an interval of plausible values, derived from the natural spread of the data around the mean TF relation. We call this the statistical uncertainty, σ_{stat} . Estimate the statistical uncertainty if $log_{10}(V_{\text{max}})$ is inferred from *K* using the TF relation from question 1.2. For this, consider for each point the difference between the value of $log_{10}(V_{\text{max}})$ estimated from *K* using your linear fit and the actual measurement of $log_{10}(V_{\text{max}})$, and take σ_{stat} as two times the root mean square (RMS) of these differences[†].

$\sigma_{stat} = ?$

 $^{\dagger} \text{The RMS}$ of a set of values is the square root of the arithmetic mean of the squares of those values.

4.3 Recalculate the exponent in the scaling relation $\frac{M_{tot1}}{M_{tot2}} = 10^g$, expressing g as an 10.0pt interval estimated by considering the extreme possible variations arising from both the systematic and statistical uncertainties:







Data Analysis 2: Stars and Exoplanets (75 points)

Please read the general instructions in the separate envelope before you start this problem.

In this problem, we will explore the connection between the physical properties of exoplanets and their host stars and will use the observational data to discover as much as possible about these systems. You may neglect interstellar extinction.

Part 1 (20 points).

Name of planet	Name of star	$T_{eff}\left(K\right)$	$g~(ms^{-2})$	m_v (magnitudes)	parallax (milliarcsec)
Gorgona	$HD\ 209458$	5980	347	7.63	20.67

Table 1: Observational data for exoplanet Gorgona and its parent star HD 209458

The effective temperature (T_{eff}) and the gravitational acceleration in the surface of the star (g) can be measured from the shape of the spectrum and its absorption lines. The visual apparent magnitude (m_v) and parallax are measured by doing photometry and astrometry, respectively.

Additionally, it has been observed that every 3.52 days the brightness of the star drops due to the transit of the planet in front of it, as it is represented in this lightcurve:







Part 2 (25 points).

The habitable zone is defined as the region in which a planet may have liquid water on its surface. This is mainly related to the amount of radiation received from the host star, which must be within some limits to ensure a favorable range of planet surface temperatures.

We define the effective flux received by a planet as $S_{eff} = \frac{L}{a^2}$, where L is the star luminosity in solar units, and a is the mean orbital radius in au. The minimum flux in the habitable zone can be approximated by $S_{min} = S_{eff_{\odot}} + n \cdot T_{\star} + b \cdot T_{\star}^2 + c \cdot T_{\star}^3 + d \cdot T_{\star}^4$, where $T_{\star} = (T_{eff} - T_{eff_{\odot}})$, and $S_{eff_{\odot}}$ is the equivalent flux for the case of the Sun, which along with the coefficients n, b, c, d is given in the following table. The maximum flux for habitability, S_{max} , is found with the same equation but different constants:





Constant	S_{max}	S_{min}
$S_{eff_{\odot}}$	1.0512	0.3438
n	1.3242×10^{-4}	5.8942×10^{-5}
b	1.5418×10^{-8}	1.6558×10^{-9}
с	-7.9895×10^{-12}	-3.0045×10^{-12}
d	-1.8328×10^{-15}	-5.2983×10^{-16}

The table below gives real data for 7 different star-planet systems. However planet names have been changed to honour some natural sanctuaries in Colombia:

Stellar P	arameters	Planet Paran	neters
$T_{eff}\left[K\right]$	$M_V\left[mag\right]$	Name	a[au]
6180	3.68	Tayrona	0.04
5730	3.87	Iguaque	0.04
5980	4.21	Gorgona	0.04
5480	6.04	Amacayacu	0.08
5770	3.48	Malpelo	0.05
6130	3.07	Pisba	0.03
6140	3.85	Tatamá	0.06

2.1 In the following figure, the vertical axis represents the effective temperature of stars, and the horizontal axis represents the effective flux received by orbiting planets. The dot marked on the graph represents planet Earth, and dashed lines mark the limits of the habitable zone.







2.2 Now considering the real orbital radius given in the table for each planet, indicate with YES or NO which of them are in the habitable zone. Show your quantitative reasoning on the working sheets.

Planet's Name	In habitable zone? YES / NO	
Tayrona		
Iguaque		
Gorgona		
Amacayacu		
Malpelo		
Pisba		
Tatamá		



Part 3 (30 points).

In the last page you find a list of 38 exoplanets, and the goal is to find out if low-mass exoplanets (LME) and high-mass exoplanets (HME) tend to orbit around stars with different characteristics.

3.1 To get a robust low-mass subsample one can apply a technique called "iterative sigma-clipping". The idea is to compute the mean (μ) and the standard deviation (σ) of the masses and to exclude from the sample, those planets with masses above $\mu + \sigma$. Then repeat the same steps with the remaining subsample two more times. We will say that planets in the final subsample are the low-mass ones, and those excluded during the iterations, the high-mass ones. Fill the following table with the numbers you find in the process:

Low-mass sample	Sample size	μ	σ	$\mu + \sigma$	No. of planets to exclude
Full / Original	38				
subsample after 1st iteration					
subsample after 2nd iteration					
subsample after final iteration					

- **3.2** Make a plot using the X-axis for the serial number of the planets in the list (1, 2, 3, ...), and the Y-axis for the mass of the planets. Mark 3 horizontal lines at the $\mu + \sigma$ thresholds you found in the iterations:
- **3.3** Let's investigate the possible difference in the effective temperatures of host 10.0pt stars in both groups, computing some descriptive statistics:

	Min.	1st Quartile	Median 2nd quartile	3rd Quartile	Max
LME					
HME					











No	Name of Dianot	Planet	T_{eff} of the
NO.	Name of Flamet	Mass $[M_J]$	Host Star

	_		
1	KEPLER-37 b	0.01	5520
2	KEPLER-21 b	0.02	6256
3	HD 97658 b	0.02	5468
4	HD 46375 b	0.23	5345
5	HD 219134 h	0.28	5209
6	HD 88133 b	0.30	5582
7	HD33283 b	0.33	5877
8	HD 149026 b	0.36	6096
9	BD-10 3166 b	0.46	5578
10	HD 75289 b	0.47	6196
11	HD 217014 b	0.47	5755
12	HD 2638 b	0.48	5564
13	WASP-13 b	0.49	6025
14	WASP-34 b	0.59	5771
15	HD 209458 b	0.69	5988
16	HAT-P-30 b	0.71	6177
17	WASP-76 b	0.92	6133
18	WASP-74 b	0.97	5727
19	HAT-P-6 b	1.06	6442
20	HD189733 b	1.14	5374
21	WASP-82 b	1.24	6257
22	KELT-7 b	1.29	6460
23	HD 149143 b	1.33	6067
24	KELT-3 b	1.42	6404
25	KELT-2A b	1.49	6164
26	HD86081 b	1.50	6015
27	HAT-P-7 b	1.74	6270
28	HD 118203 b	2.14	5847
29	HAT-P-14 b	2.20	6490
30	WASP-38 b	2.71	6178
31	HD17156 b	3.20	5985
32	KELT-6 c	3.71	6176
33	HD 75732 d	3.86	5548
34	HD 115383 b	4.00	5891
35	HD 120136 b	5.84	6210
36	WASP-14 b	7.34	6195
37	HAT-P-2 b	8.74	6439
38	XO-3 b	11.79	6281

Night Observation and Simulated Sky

Points: 75p

Authors: Ángela Pérez, Wilder Reyes, Alvaro José Cano, Orlando Mendez,

Carlos Molina, Camilo Delgado-Correal & Alfonso Hiram Redondo (Academic Committee

for simulated sky test)

Topic: Observation

Click to START





10 seconds to GO



Image 1Question: 1.1Time: 2minutes





Image 2 Question: 1.2 Time: 2 minutes





Image 3Question: 1.3Time: 3minutes





No Image Questions: 1.4, 1.5 and 1.6 Time: 8 minutes



The projected sky corresponds to **-30° of latitude** (South) with **-74 ° longitude** (West).

Image 4 Identify this part of the sky and prepare...



The projected sky corresponds to -30° of latitude (South) with -74 ° longitude (West). Image 4 Questions: 1.7 Time: 2 minutes





The projected sky corresponds to -30° of latitude (South) with -74 ° longitude (West). Image 4 Question: 1.8 Time: 2 minutes





Correction in answer sheet:

The projected sky corresponds to -30° of latitude (South) with -74 ° longitude (West). Image 4 Question: 1.9 Time: 3 minutes





The projected sky corresponds to -30° of latitude (South) with -74 ° longitude (West). Image 4 Question: 1.10 Time: 3 minutes





Image5Questions: 1.11 and 1.12Time: 4 minutes





Image6Question:1.13Time:2 minutes





Image7Question:1.14Time:2 minutes



Image8Question:1.15Time:2 minutes



Identify this part of the sky and prepare to recognize some stars and objects

Image 9 Star 1 Question: 1.16 Time: 1 min x star

Image 9 Star 2 Question: 1.16 Time: 1 min x star

Image 9 Star 3 Question: 1.16 Time: 1 min x star

Image 9 Star 4 Question: 1.16 Time: 1 min x star Image 10 Object 1 Question: 1.17 Time: 1 min x object Image 10 Object 2 Question: 1.17 Time: 1 min x object Image 10 Object 3 Question: 1.17 Time: 1 min x object Image 10 Object 4 Question: 1.17 Time: 1 min x object

The End

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